

Elasticities of Demand :-

There are as many elasticities of demand as its determinants. The most important of these elasticities is (A) The price elasticity of demand :-

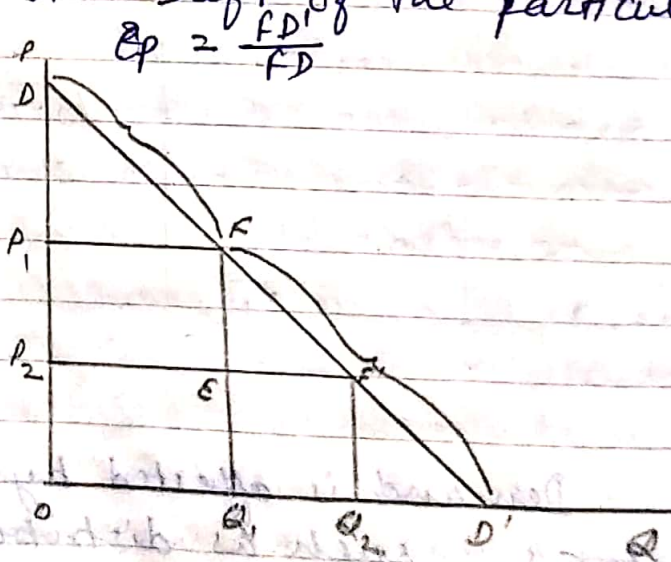
Elasticity of demand is defined as the proportionate change in quantity demanded resulting from a very small ^{proportionate} change in price.

$$E_p = \frac{\frac{dQ}{Q}}{\frac{dP}{P}}$$

or

$$E_p = \frac{dQ}{dP} \times \frac{P}{Q}$$

The elasticity changes at the various points of the linear demand curve. The point elasticity of a linear demand curve is shown by the ratio of the segments of the line to the right and to the left of the particular point



Proof :- $\Delta P = P_1 - P_2 = EF$, $\Delta Q = Q_1 - Q_2 = EF'$

$P = OP_1$, $Q = OQ_1$

$$E_p = \frac{EF'}{EF} \cdot \frac{OP_1}{OQ_1}$$

From fig triangles FEF' and $FD'D'$ are similar. Hence

$$\frac{EF'}{EF} = \frac{Q_1 D'}{P_1 D'} = \frac{Q_1 D'}{OP_1} \dots 3$$

$$e_p = \frac{Q_1 D'}{OQ_1} \cdot \frac{OQ_1}{OQ_1} = \frac{Q_1 D'}{OQ_1}$$

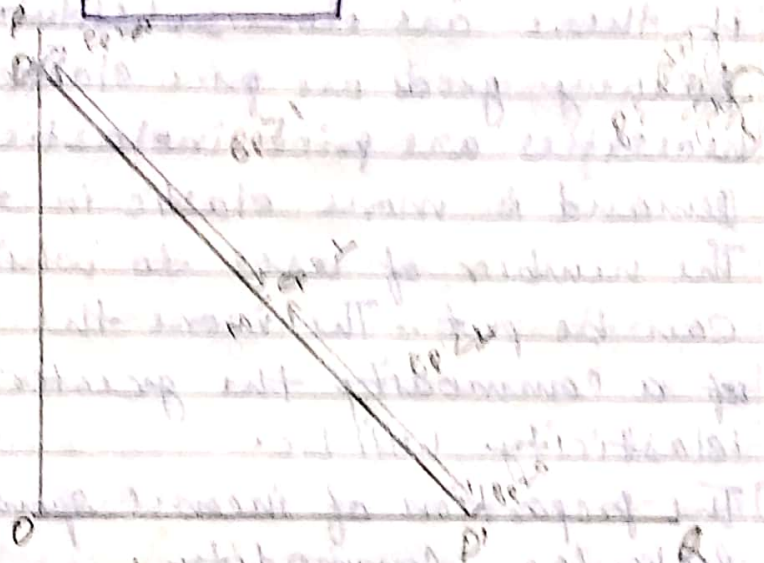
the triangles OPF and $FQ_1 D'$ are similar, so

$$\frac{Q_1 D'}{FD'} = \frac{PF}{FD} = \frac{OQ_1}{FD}$$

Rearranging we obtain

$$\frac{Q_1 D'}{OQ_1} = \frac{FD'}{FD}$$

$$e_p = -\frac{FD'}{FD}$$



In fig. A linear demand curve $e_p \perp$ at point M . any point to the right of M the $e_p < 1$ and left of M $e_p > 1$ at point D $e_p \rightarrow \infty$ and at point D' $e_p = 0$. The price elasticity is always negative because of the inverse relationship between Q and P implied by law of Demand.

- If $e_p = 0$ the demand is perfectly inelastic.
- If $e_p = 1$ the demand is unitary elastic.
- If $e_p = \infty$ the demand is perfectly elastic.
- If $0 < e_p < 1$ the demand is inelastic.
- If $1 < e_p < \infty$ the demand is elastic.